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### **Iso-S-Closedness and Iso-S\*-Closedness in L-Fuzzy Topological Spaces**

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#### **ABSTRACT**

Along the line of compactness in L-fuzzy topological spaces, we introduce iso-S-closeness and iso-S\*-closeness for arbitrary L-fuzzy subsets. Further CL-iso-S-closed and CL-iso-S\*-closed L-fuzzy spaces are defined and studied some of the properties and obtain some relations of these spaces with other spaces.

**KEYWORDS:** L-fuzzy compactness, L-fuzzy CL-iso-S-closedness, L-fuzzy CL-iso-S\*-closedness.

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## INTRODUCTION

In  $[0,1]$  fuzzy topological space,  $S$ -closedness and  $S^*$ -closedness were defined by Coker<sup>10</sup> and Malakar<sup>15</sup>, but the definitions are not studied in arbitrary fuzzy sets. Later Kudri and Warner<sup>13</sup> and Kudri<sup>14</sup> have introduced good definitions of  $S$ -closedness and  $S^*$ -closedness in  $L$ -fuzzy topological spaces where  $L$  is a fuzzy lattice and have studied some of their properties along the line of compactness<sup>11</sup>. In 1970, Bacon<sup>3</sup> introduced the notion of isocompactness in general topology. Bhaumik and Bhattacharya<sup>5</sup> introduced isocompactness in  $L$ -fuzzy topological spaces, in which every  $L$ -fuzzy closed, countably compact subspaces are  $L$ -fuzzy compact. In this paper, using the concepts of  $S$ -closedness and  $S^*$ -closedness in  $L$ -fuzzy topological spaces we introduce two new concepts namely iso- $S$ -closedness and iso- $S^*$ -closedness for arbitrary  $L$ -fuzzy subsets and study some properties of these spaces. Further we generalize these concepts as  $CL$ -iso- $S$ -closedness and  $CL$ -iso- $S^*$ -closedness in  $L$ -fuzzy topological spaces which are the stronger form of iso- $S$ -closedness and iso- $S^*$ -closedness.

## PRILIMINARIES

Throughout this paper  $X$  and  $Y$  will be non-empty ordinary sets and  $L = L ( \leq, \vee, \wedge, ' )$  will denote a fuzzy lattice, i.e. a completely distributive lattice with a smallest element  $0$  and a largest element  $1 (0 \neq 1)$ , and with an order reversing involution  $a \rightarrow a'$  ( $a \in L$ ). An  $L$ -fuzzy subset on  $X$  is a mapping  $\lambda : X \rightarrow L$ , and the family of  $L$ -fuzzy subsets on  $X$  is denoted by  $L^X$ .  $X$  is called the carrier domain of each  $L$ -fuzzy subset on  $X$ .

**Definition 2.1** An element  $p$  of  $L$  is called prime<sup>1</sup> if and only if  $p \neq 1$  and whenever  $a, b \in L$  with  $a \wedge b \leq p$  then  $a \leq p$  or  $b \leq p$ . The set of all prime elements of  $L$  will be denoted by  $pr(L)$ .

**Definition 2.2** An element  $\alpha$  of  $L$  is called union-irreducible or coprime<sup>1</sup> if and only if whenever  $a, b \in L$  with  $\alpha \leq a \vee b$  then  $\alpha \leq a$  or  $\alpha \leq b$ . The set of all nonzero union-irreducible elements of  $L$  will be denoted by  $M(L)$ . It is obvious that  $p \in pr(L)$  if and only if  $p' \in M(L)$ .

**Definition 2.3** Let  $(X, \tau)$  be an  $L$ -fuzzy topological space and let  $\lambda \in L^X$ . The  $L$ -fuzzy set  $\lambda$  is called

- i) Semiopen<sup>2</sup> if and only if there exists  $\beta \in \tau$  such that  $\beta \leq \lambda \leq cl(\beta)$  and semiclosed<sup>2</sup> if and only if there exists a closed  $L$ -fuzzy set  $\beta$  such that  $int(\beta) \leq \lambda \leq \beta$  that is  $\lambda'$  is semiopen
- ii) Pre-open<sup>13</sup> if and only if  $\lambda \leq int(cl(\lambda))$  and pre-closed<sup>13</sup> if and only if  $cl(int(\lambda)) \leq \lambda$  that is  $\lambda'$  is pre-open.
- iii) Regularly open<sup>2</sup> if and only if  $\lambda = int(cl(\lambda))$  and  $\lambda$  is regularly closed<sup>2</sup> if and only if  $\lambda'$

is regularly open i.e.,  $\lambda = \text{cl}(\text{int}(\lambda))$ .

- iv) Regularly semiopen<sup>2</sup> if and only if there exist a regularly open L-fuzzy set  $\beta$  such that  $\beta \leq \lambda \leq \text{cl}(\beta)$  and  $\lambda$  is regularly semiclosed<sup>2</sup> if and only if  $\lambda'$  is regularly semiopen.

**Definition 2.4** Let  $(X, \tau)$  and  $(Y, \tau')$  be two L-fuzzy topological spaces. A function  $f : (X, \tau) \rightarrow (Y, \tau')$  is called

- i) Almost continuous<sup>2</sup> if and only if  $f^{-1}(\lambda) \in \tau$  for all regularly open  $\lambda$  in  $(Y, \tau')$ .
- ii) Almost open<sup>13</sup> if and only if  $f(\lambda) \in \tau'$  for every regularly open  $\lambda$  in  $(X, \tau)$ .
- iii) Weakly continuous<sup>2</sup> if and only if  $f^{-1}(\lambda) \leq \text{int}(f^{-1}(\text{cl}(\lambda)))$  for all  $\lambda \in \tau'$ .
- iv) Semi-weakly continuous<sup>10</sup> if and only if  $f^{-1}(\lambda) \leq \text{int}^*(f^{-1}(\text{cl}^*(\lambda)))$  for all semiopen  $\lambda \in \tau'$ .
- v) Irresolute<sup>10</sup> if and only if  $f^{-1}(\lambda)$  is semi-open in  $(X, \tau)$  for every semi-open L-fuzzy set  $\lambda$  in  $(Y, \tau')$ .
- vi) Semi-irresolute<sup>15</sup> if and only if  $f^{-1}(\lambda)$  is semiclopen in  $(X, \tau)$  for every semiclopen L-fuzzy set  $\lambda$  in  $(Y, \tau')$ .
- vii) Perfect<sup>17</sup> if and only if  $f$  is L-fuzzy continuous, L-fuzzy closed and for each  $y \in Y$ ,  $f^{-1}(y)$  is compact L-fuzzy subset in  $(X, \tau)$ .

**Definition 2.5** Let  $(X, \tau)$  be an L-fuzzy topological space and  $\lambda \in L^X$ . Then

- i) The L-fuzzy subset  $\lambda$  is said to be compact<sup>12</sup> if and only if for every  $p \in \text{Pr}(L)$  and every collection  $(\gamma_i)_{i \in J}$  of open L-fuzzy subsets with  $(\bigvee_{i \in J} \gamma_i)(x) \not\leq p$  for all  $x \in X$  with  $\lambda(x) \geq p'$ , there exists a finite subset  $F$  of  $J$  with  $(\bigvee_{i \in F} \gamma_i)(x) \not\leq p$  for all  $x \in X$  with  $\lambda(x) \geq p'$ .  
If  $\lambda$  is the whole space, then we say that the L-fuzzy topological space  $(X, \tau)$  is compact.
- ii) The L-fuzzy subset  $\lambda$  is said to be semicompact<sup>14</sup> if and only if for every  $p \in \text{Pr}(L)$  and every collection  $(\gamma_i)_{i \in J}$  of semiopen L-fuzzy subsets with  $(\bigvee_{i \in J} \gamma_i)(x) \not\leq p$  for all  $x \in X$  with  $\lambda(x) \geq p'$ , there exists a finite subset  $F$  of  $J$  with  $(\bigvee_{i \in F} \gamma_i)(x) \not\leq p$  for all  $x \in X$  with  $\lambda(x) \geq p'$ .

If  $\lambda$  is the whole space, then we say that the L-fuzzy topological space  $(X, \tau)$  is semicompact.

- iii) The L-fuzzy subset  $\lambda$  is said to be S-closed<sup>13</sup> if and only if for every  $p \in \text{Pr}(L)$  and every collection  $(\gamma_i)_{i \in J}$  of semiopen L-fuzzy subsets with  $(\bigvee_{i \in J} \gamma_i)(x) \not\leq p$  for all  $x \in X$  with  $\lambda(x) \geq p'$ , there exists a finite subset  $F$  of  $J$  with  $(\bigvee_{i \in F} \text{cl} \gamma_i)(x) \not\leq p$  for all  $x \in X$  with  $\lambda(x) \geq p'$ .

If  $\lambda$  is the whole space, then we say that the L-fuzzy topological space  $(X, \tau)$  is S-closed.

iv) The L-fuzzy subset  $\lambda$  is said to be  $S^*$ -closed<sup>14</sup> if and only if for every  $p \in \text{Pr}(L)$  and every collection  $(\gamma_i)_{i \in J}$  of semi-open L-fuzzy subsets with  $(\bigvee_{i \in J} \gamma_i)(x) \not\leq p$  for all  $x \in X$  with  $\lambda(x) \geq p'$ , there exists a finite subset  $F$  of  $J$  with  $(\bigvee_{i \in F} \text{cl}^*(\gamma_i))(x) \not\leq p$  for all  $x \in X$  with  $\lambda(x) \geq p'$ .

If  $\lambda$  is the whole space, then we say that the L-fuzzy topological space  $(X, \tau)$  is  $S^*$ -closed.

Other characterizations of  $S$ -closedness and  $S^*$ -closed are given in Th.2.6, Th. 2.7 and Th. 2.8.

**Theorem 2.6** Let  $(X, \tau)$  be an L-fuzzy topological space and  $\lambda \in L^X$ . The L-fuzzy subset  $\lambda$  is  $S$ -closed<sup>13</sup> if and only if for every  $p \in \text{Pr}(L)$  and every collection  $(\gamma_i)_{i \in J}$  of regularly closed L-fuzzy sets with  $(\bigvee_{i \in J} \gamma_i)(x) \not\leq p$  for all  $x \in X$  with  $\lambda(x) \geq p'$ , there is a finite subset  $F$  of  $J$  with  $(\bigvee_{i \in F} \gamma_i)(x) \not\leq p$  for all  $x \in X$  with  $\lambda(x) \geq p'$ .

**Theorem 2.7** Let  $(X, \tau)$  be an L-fuzzy topological space and  $\lambda \in L^X$ . The L-fuzzy subset  $\lambda$  is  $S$ -closed<sup>13</sup> if and only if for every  $p \in \text{Pr}(L)$  and every collection  $(\gamma_i)_{i \in J}$  of regularly semiopen L-fuzzy sets with  $(\bigvee_{i \in J} \gamma_i)(x) \not\leq p$  for all  $x \in X$  with  $\lambda(x) \geq p'$ , there is a finite subset  $F$  of  $J$  with  $(\bigvee_{i \in F} \text{cl} \gamma_i)(x) \not\leq p$  for all  $x \in X$  with  $\lambda(x) \geq p'$ .

**Theorem 2.8** Let  $(X, \tau)$  be an L-fuzzy topological space and  $\lambda \in L^X$ . The L-fuzzy subset  $\lambda$  is  $S^*$ -closed<sup>14</sup> if and only if for every  $p \in \text{Pr}(L)$  and every collection  $(\gamma_i)_{i \in J}$  of semiclopen L-fuzzy sets with  $(\bigvee_{i \in J} \gamma_i)(x) \not\leq p$  for all  $x \in X$  with  $\lambda(x) \geq p'$ , there is a finite subset  $F$  of  $J$  with  $(\bigvee_{i \in F} \gamma_i)(x) \not\leq p$  for all  $x \in X$  with  $\lambda(x) \geq p'$ .

**Definition 2.9** Let  $(X, \tau)$  be an L-fuzzy topological space and  $\lambda \in L^X$ . The L-fuzzy subset  $\lambda$  is said to be L-fuzzy isocompact<sup>5</sup> if every countably compact and closed L-fuzzy subset of  $\lambda$  is L-fuzzy compact.

If  $\lambda$  is the whole space, then L-fuzzy topological space  $(X, \tau)$  is isocompact.

**Definition 2.10** Let  $(X, \tau)$  be an L-fuzzy topological space and  $\lambda \in L^X$ . The L-fuzzy subset  $\lambda$  is said to be semi-isocompact<sup>8</sup> if and only if every countably compact and closed L-fuzzy subset of  $\lambda$  is semi compact. If  $\lambda$  is the whole space, then the L-fuzzy topological space  $(X, \tau)$  is also semi-isocompact.

**Theorem 2.11**<sup>13</sup> Let  $(X, \tau)$  be an  $S$ -closed L-fuzzy topological space. Then each regularly open L-fuzzy subset in  $(X, \tau)$  is  $S$ -closed.

**Theorem 2.12<sup>13</sup>** Let  $(X, \tau)$  and  $(Y, \tau')$  be L-fuzzy topological spaces and let  $f : (X, \tau) \rightarrow (Y, \tau')$  be an almost continuous, almost open mapping and let  $\lambda$  be an S-closed L-fuzzy subset of  $(X, \tau)$ . Then  $f(\lambda)$  is an S-closed L-fuzzy subset of  $(Y, \tau')$ .

**Proposition 2.13<sup>14</sup>** Let  $(X, \tau)$  and  $(Y, \tau')$  be L-fuzzy topological spaces and let  $f : (X, \tau) \rightarrow (Y, \tau')$  be a semi-irresolute mapping with  $f^{-1}(y)$  is finite for every  $y \in Y$ . If  $\lambda \in L^X$  is  $S^*$ -closed in  $(X, \tau)$ , then  $f(\lambda)$  is  $S^*$ -closed in  $(Y, \tau')$ .

**Proposition 2.14<sup>14</sup>** Let  $(X, \tau)$  and  $(Y, \tau')$  be L-fuzzy topological spaces and let  $f : (X, \tau) \rightarrow (Y, \tau')$  be an irresolute mapping with  $f^{-1}(y)$  is finite for every  $y \in Y$ . If  $\lambda \in L^X$  is  $S^*$ -closed in  $(X, \tau)$ , then  $f(\lambda)$  is  $S^*$ -closed in  $(Y, \tau')$ .

**Proposition 2.15<sup>14</sup>** Let  $(X, \tau)$  and  $(Y, \tau')$  be L-fuzzy topological spaces and let  $f : (X, \tau) \rightarrow (Y, \tau')$  be a semi-irresolute mapping with  $f^{-1}(y)$  is finite for every  $y \in Y$ . If  $\lambda \in L^X$  is semicompact in  $(X, \tau)$ , then  $f(\lambda)$  is  $S^*$ -closed in  $(Y, \tau')$ .

**Proposition 2.16<sup>14</sup>** Let  $(X, \tau)$  and  $(Y, \tau')$  be L-fuzzy topological spaces and let  $f : (X, \tau) \rightarrow (Y, \tau')$  be a semiweekly continuous mapping with  $f^{-1}(y)$  is finite for every  $y \in Y$ . If  $\lambda \in L^X$  is semicompact in  $(X, \tau)$ , then  $f(\lambda)$  is  $S^*$ -closed in  $(Y, \tau')$ .

**Theorem 2.17<sup>2</sup>** If  $\lambda$  is an L-fuzzy subset of  $(X, \tau)$ ,  $\mu$  is an L-fuzzy subset of  $(Y, \tau')$  and  $X$  is product related to  $Y$ , then

- a)  $Cl(\lambda \times \mu) = Cl\lambda \times Cl\mu$  and
- b)  $Int(\lambda \times \mu) = Int\lambda \times Int\mu$  hold.

**Definition 2.18** An L-fuzzy topological space  $(X, \tau)$  is called fully stratified<sup>17</sup> if for each  $p \in L$ , the L-fuzzy set which takes constant value  $p$  at each point  $x \in X$  belongs to  $\tau$ .

**Theorem 2.19<sup>17</sup>** If  $(X, \tau)$  be a compact L-fuzzy topological space and  $(Y, \tau')$  be a fully stratified L-fuzzy topological space, then the projection mapping  $P_Y: X \times Y \rightarrow Y$  is L-fuzzy perfect.

### **ISO-S-CLOSEDNESS AND ISO-S\*-CLOSEDNESS IN L-FUZZY TOPOLOGICAL SPACES**

**Definition 3.1** Let  $(X, \tau)$  be an L-fuzzy topological space and  $\lambda \in L^X$ . The L-fuzzy subset  $\lambda$  is said to be iso-S-closed if and only if every closed countably compact subset of  $\lambda$  is S-closed.

If  $\lambda$  is the whole space, then the L-fuzzy topological space  $(X, \tau)$  is also iso-S-closed.

**Theorem 3.2**

Let  $(X, \tau)$  be an L-fuzzy topological space and  $\lambda \in L^X$ . Then the L-fuzzy subset  $\lambda$  is iso-S-closed if and only if every regular closed countably compact subset of  $\lambda$  is S-closed.

**Proof:** Since each regular closed set is closed then the result follows immediately from the definition 3.1.

**Theorem 3.3**

If an L-fuzzy topological space  $(X, \tau)$  is the union of a countable collection of closed and iso-S-closed L-fuzzy subsets, then  $(X, \tau)$  is L-fuzzy iso-S-closed.

**Proof:** Suppose  $X = \bigvee \mu_i$ , where each  $\mu_i$  is closed and iso-S-closed L-fuzzy subset of  $X$  and let  $\beta$  be a closed and countably compact L-fuzzy subset of  $X$ . Let  $p \in \text{pr}(L)$  and let  $\{\gamma_i\}_{i \in J}$  be a family of semi-open L-fuzzy sets with  $(\bigvee_{i \in J} \gamma_i)(x) \not\geq p$  for all  $x \in X$  such that  $\beta(x) \geq p'$ . For each  $i$ ,  $\beta \wedge \mu_i$  is a closed, countably compact L-fuzzy subset of  $\mu_i$ . So it is S-closed L-fuzzy subset, since each  $\mu_i$  is L-fuzzy iso-S-closed. By S-closedness of  $\beta \wedge \mu_i$ , there exist a finite subset  $F$  of  $J$  with  $(\bigvee_{i \in F} \gamma_i)(x) \not\geq p$  for all  $x \in X$  such that  $(\beta \wedge \mu_i)(x) \geq p'$  i.e.  $\beta(x) \geq p'$ . Hence  $\beta$  is a S-closed L-fuzzy subset, which implies that  $X$  is L-fuzzy iso-S-closed.

**Theorem 3.4**

Let  $f : (X, \tau) \rightarrow (Y, \tau')$  be an L-fuzzy perfect, almost continuous and almost open mapping from an iso-S-closed L-fuzzy topological space  $(X, \tau)$  onto an L-fuzzy topological space  $(Y, \tau')$ . Then  $(Y, \tau')$  is L-fuzzy iso-S-closed.

**Proof :** Let  $\beta$  be a regular closed and countably compact L-fuzzy subset of  $(Y, \tau')$ . Since  $f$  is L-fuzzy perfect map, then  $f^{-1}(\beta)$  is closed and countably compact L-fuzzy subset of  $(X, \tau)$ . By L-fuzzy iso-S-closedness of  $(X, \tau)$ ,  $f^{-1}(\beta)$  is L-fuzzy S-closed. Since  $f$  is onto L-fuzzy almost continuous and almost open mapping then  $ff^{-1}(\beta) = \beta$  is S-closed [by 2.12] L-fuzzy subset in  $(Y, \tau')$ . Hence  $(Y, \tau')$  is L-fuzzy iso-S-closed.

**Theorem 3.5**

If  $(X, \tau)$  and  $(Y, \tau')$  be two S-closed L-fuzzy topological spaces such that  $X$  is product related to  $Y$ , then  $X \times Y$  is L-fuzzy S-closed.

**Proof:** Let  $\{\lambda_i \times \beta_i : i \in I\}$  be an L-fuzzy cover of  $X \times Y$  by semi-open L-fuzzy sets of  $X \times Y$ , where  $\lambda_i$ 's and  $\beta_i$ 's are semi-open L-fuzzy sets in  $X$  and  $Y$  respectively. Then  $\{\lambda_i : i \in I\}$  and  $\{\beta_i : i \in I\}$  are L-fuzzy semi-open covers of  $X$  and  $Y$  respectively. As  $(X, \tau)$  and  $(Y, \tau')$  are S-closed L-fuzzy

topological spaces then there exist finite subsets  $M$  and  $N$  of  $I$  such that,  $(\bigvee_{i \in M} (\text{cl}\lambda_i)) (x) \not\leq p$  and  $(\bigvee_{i \in N} (\text{cl}\beta_i)) (x) \not\leq p$ .

Now,  $\{\bigvee \text{cl}(\lambda_i \times \beta_i) : i \in M \vee N\} (x) = [\bigvee \{\text{cl} \lambda_i : i \in M \vee N\}] (x) \times [\bigvee \{\text{cl} \beta_i : i \in M \vee N\}] (x) \not\leq p$

Hence the proof.

**Theorem 3.6**

Let  $(X, \tau)$  be an  $S$ -closed  $L$ -fuzzy topological space and  $(Y, \tau')$  be a fully stratified iso- $S$ -closed  $L$ -fuzzy topological space such that  $X$  is product related to  $Y$ . Then  $X \times Y$  is  $L$ -fuzzy iso- $S$ -closed.

**Proof:** Let  $(X, \tau)$  be an  $S$ -closed  $L$ -fuzzy topological space and  $(Y, \tau')$  be a fully stratified iso- $S$ -closed  $L$ -fuzzy topological space and consider the projection map  $P_Y : X \times Y \rightarrow Y$ .

Let  $\beta$  be a countably compact, closed  $L$ -fuzzy subset of  $X \times Y$ .  $P_Y(\beta)$  is countably compact and closed  $L$ -fuzzy subset as  $P_Y$  being  $L$ -fuzzy continuous. By  $L$ -fuzzy iso- $S$ -closedness of  $(Y, \tau')$ ,  $P_Y(\beta)$  is  $S$ -closed  $L$ -fuzzy subset of  $(Y, \tau')$ . Thus by 3.5,  $X \times P_Y(\beta)$  is  $L$ -fuzzy  $S$ -closed. So  $\beta$  is  $L$ -fuzzy countably compact, closed subset of  $X \times P_Y(\beta) \leq X \times Y$ , and is  $S$ -closed  $L$ -fuzzy subset of  $X \times Y$ . Hence  $X \times Y$  is  $L$ -fuzzy iso- $S$ -closed.

**Definition 3.7** An  $L$ -fuzzy topological space  $(X, \tau)$  is called hereditarily iso- $S$ -closed if every subspace of it is iso- $S$ -closed.

**Theorem 3.8**

Let  $(X, \tau)$  be a fully stratified iso- $S$ -closed  $L$ -fuzzy topological space and  $(Y, \tau')$  be a hereditarily iso- $S$ -closed  $L$ -fuzzy topological space such that  $X$  is product related to  $Y$ . Then  $X \times Y$  is  $L$ -fuzzy iso- $S$ -closed.

**Proof:** Let  $(X, \tau)$  be a fully stratified iso- $S$ -closed  $L$ -fuzzy topological space and  $(Y, \tau')$  be a hereditarily  $L$ -fuzzy iso- $S$ -closed space. Let us consider the projection map  $P_Y : X \times Y \rightarrow Y$ .

Let  $\beta$  be a countably compact, closed  $L$ -fuzzy subset of  $X \times Y$ . Then  $P_Y(\beta)$  is countably compact  $L$ -fuzzy subset of  $(Y, \tau')$ . Since  $(Y, \tau')$  is hereditarily iso- $S$ -closed  $L$ -fuzzy topological space then  $P_Y(\beta)$  is  $L$ -fuzzy  $S$ -closed. Thus from 3.6,  $X \times P_Y(\beta)$  is  $L$ -fuzzy iso- $S$ -closed. Since  $\beta$  is a countably compact and closed subset of  $X \times P_Y(\beta) \leq X \times Y$ ,  $\beta$  is  $L$ -fuzzy  $S$ -closed subset of  $X \times Y$ . Hence  $X \times Y$  is  $L$ -fuzzy iso- $S$ -closed.

**Definition 3.9** Let  $(X, \tau)$  be an  $L$ -fuzzy topological space and  $\lambda \in L^X$ . The  $L$ -fuzzy subset  $\lambda$  is said to be iso- $S^*$ -closed if and only if every closed countably compact subset of  $\lambda$  is  $S^*$ -closed.

If  $\lambda$  is the whole space, then the  $L$ -fuzzy topological space  $(X, \tau)$  is also iso- $S^*$ -closed.

**Theorem 3.10**

If an L- fuzzy topological space  $(X, \tau)$  is the union of a countable collection of closed and iso-  $S^*$ -closed L-fuzzy subsets, then  $(X, \tau)$  is L-fuzzy iso-  $S^*$ -closed.

**Proof:** Suppose  $X = \bigvee \mu_i$ , where each  $\mu_i$  is closed and iso- $S^*$ -closed L-fuzzy subset of  $X$  and let  $\beta$  be a closed and countably compact L-fuzzy subset of  $X$ . Let  $p \in \text{pr}(L)$  and let  $\{\gamma_i\}_{i \in J}$  be a family of semi-open L-fuzzy sets with  $(\bigvee_{i \in J} (\gamma_i))(x) \not\leq p$  for all  $x \in X$  such that  $\beta(x) \geq p'$ .

For each  $i$ ,  $\beta \wedge \mu_i$  is a closed, countably compact L-fuzzy subset of  $\mu_i$ . So it is  $S^*$ -closed L-fuzzy subset, since each  $\mu_i$  is L-fuzzy iso-  $S^*$ -closed. By  $S^*$ -closedness of  $\beta \wedge \mu_i$ , there exist a finite subset  $F$  of  $J$  with  $(\bigvee_{i \in F} (\text{cl} * \gamma_i))(x) \not\leq p$  for all  $x \in X$  such that  $(\beta \wedge \mu_i)(x) \geq p'$  i.e.  $\beta(x) \geq p'$ . Hence  $\beta$  is  $S^*$ -closed L-fuzzy subset, which implies that  $X$  is L-fuzzy iso-  $S^*$ -closed.

**Theorem 3.11**

Let  $f : (X, \tau) \rightarrow (Y, \tau')$  be an L-fuzzy perfect and semi-irresolute mapping with  $f^{-1}(y)$  is finite for every  $y \in Y$ , from an iso-  $S^*$ -closed L-fuzzy topological space  $(X, \tau)$  onto an L-fuzzy topological space  $(Y, \tau')$ . Then  $(Y, \tau')$  is L-fuzzy iso-  $S^*$ -closed.

**Proof:** Let  $\beta$  be a closed and countably compact L-fuzzy subset of  $(Y, \tau')$ . Since  $f$  is L-fuzzy perfect map, then  $f^{-1}(\beta)$  is closed and countably compact L-fuzzy subset of  $(X, \tau)$ . By L-fuzzy iso-  $S^*$ -closedness of  $(X, \tau)$ ,  $f^{-1}(\beta)$  is L-fuzzy  $S^*$ -closed. Since  $f$  is onto L-fuzzy semi-irresolute mapping with  $f^{-1}(y)$  is finite for every  $y \in Y$ , then  $f f^{-1}(\beta) = \beta$  is  $S^*$ -closed [by 2.13] L-fuzzy subset in  $(Y, \tau')$ . Hence  $(Y, \tau')$  is L-fuzzy iso-  $S^*$ -closed.

**Theorem 3.12**

Let  $f : (X, \tau) \rightarrow (Y, \tau')$  be an L-fuzzy perfect and irresolute mapping with  $f^{-1}(y)$  is finite for every  $y \in Y$ , from an iso-  $S^*$ -closed L-fuzzy topological space  $(X, \tau)$  onto an L-fuzzy topological space  $(Y, \tau')$ . Then  $(Y, \tau')$  is L-fuzzy iso-  $S^*$ -closed.

**Proof:** Since every irresolute mapping is semi-irresolute<sup>14</sup> then the result is obvious from proposition [2.14].



**Theorem 3.13**

Let  $f : (X, \tau) \rightarrow (Y, \tau')$  be an L-fuzzy perfect and semi-irresolute mapping with  $f^{-1}(y)$  is finite for every  $y \in Y$ , from an semi-iso-compact L-fuzzy topological space  $(X, \tau)$  onto an L- fuzzy topological space  $(Y, \tau')$ . Then  $(Y, \tau')$  is L-fuzzy iso- $S^*$ -closed.

**Proof:** With the help of proposition 2.15, we can prove this theorem similarly as 3.11.

**Theorem 3.14**

If  $f : (X, \tau) \rightarrow (Y, \tau')$  be L-fuzzy perfect and semi weakly continuous mapping with  $f^{-1}(y)$  is finite for every  $y \in Y$ , from an L-fuzzy semi-isocompact space  $(X, \tau)$  onto an L- fuzzy topological space  $(Y, \tau')$ , then  $(Y, \tau')$  is L-fuzzy iso-  $S^*$ -closed.

**Proof:** Let  $\beta$  be a closed and countably compact L-fuzzy subset of  $(Y, \tau')$ . Since  $f$  is L-fuzzy perfect map,  $f^{-1}(\beta)$  is closed and countably compact L-fuzzy subset of  $(X, \tau)$ . By L-fuzzy semi- compactness of  $(X, \tau)$ ,  $f^{-1}(\beta)$  is L-fuzzy semi-compact. By 2.16,  $ff^{-1}(\beta) = \beta$  is  $S^*$ -closed L-fuzzy subset in  $(Y, \tau')$ . Hence  $(Y, \tau')$  is L-fuzzy iso-  $S^*$ -closed.

**Theorem 3.15**

If  $(X, \tau)$  and  $(Y, \tau')$  be two  $S^*$ -closed L-fuzzy topological spaces such that  $X$  is product related to  $Y$ , then  $X \times Y$  is L-fuzzy  $S^*$ -closed.

**Proof:** Let  $\{\lambda_i \times \beta_i : i \in I\}$  be an L-fuzzy cover of  $X \times Y$  by semi-open L-fuzzy sets of  $X \times Y$ , where  $\lambda_i$ 's and  $\beta_i$ 's are semi-open L-fuzzy sets in  $X$  and  $Y$  respectively. Then  $\{\lambda_i : i \in I\}$  and  $\{\beta_i : i \in I\}$  are L-fuzzy semi-open covers of  $X$  and  $Y$  respectively. As  $(X, \tau)$  and  $(Y, \tau')$  are  $S^*$ -closed L-fuzzy topological spaces then there exist finite subsets  $M$  and  $N$  of  $I$  such that,  $(\bigvee_{i \in M} (cl * \lambda_i)) (x) \not\leq p$  and  $(\bigvee_{i \in N} (cl * \beta_i)) (x) \not\leq p$ . Now,  $\{\bigvee cl * (\lambda_i \times \beta_i) : i \in M \vee N\} (x) = [\bigvee \{cl * \lambda_i : i \in M \vee N\}] (x) \times [\bigvee \{cl * \beta_i : i \in M \vee N\}] (x) \not\leq p$ . Hence the proof.

**Theorem 3.16**

Let  $(X, \tau)$  be an  $S^*$ -closed L-fuzzy topological space and  $(Y, \tau')$  be a fully stratified iso-  $S^*$ -closed L-fuzzy topological space such that  $X$  is product related to  $Y$ . Then  $X \times Y$  is L-fuzzy iso-  $S^*$ -closed.

**Proof:** Let  $(X, \tau)$  be an  $S^*$ -closed L-fuzzy topological space and  $(Y, \tau')$  be a fully stratified iso-  $S^*$ -closed L-fuzzy topological space and consider the projection map  $P_Y : X \times Y \rightarrow Y$ .

Let  $\beta$  be a countably compact, closed L-fuzzy subset of  $X \times Y$ .  $P_Y(\beta)$  is countably compact and closed L-fuzzy subset as  $P_Y$  being L-fuzzy continuous. By L-fuzzy iso-  $S^*$ -closedness of  $(Y, \tau')$ ,  $P_Y(\beta)$  is  $S^*$ -closed L-fuzzy subset of  $(Y, \tau')$ . Thus by 3.15,  $X \times P_Y(\beta)$  is L-fuzzy  $S^*$ -closed. So  $\beta$  is L-fuzzy countably compact, closed subset of  $X \times P_Y(\beta) \leq X \times Y$ , and is  $S^*$ -closed L-fuzzy subset of  $X \times Y$ . Hence  $X \times Y$  is L-fuzzy iso-  $S^*$ -closed.

**Definition 3.17** An L-fuzzy topological space  $(X, \tau)$  is called hereditarily iso-  $S^*$ -closed if every sub space of it is iso-  $S^*$ -closed.

**Theorem 3.18**

Let  $(X, \tau)$  be a fully stratified iso-  $S^*$ -closed L-fuzzy topological space and  $(Y, \tau')$  be a hereditarily iso-  $S^*$ -closed L-fuzzy topological space such that  $X$  is product related to  $Y$ . Then  $X \times Y$  is L-fuzzy iso-  $S^*$ -closed.

**Proof:** Let  $(X, \tau)$  be a fully stratified iso-  $S^*$ -closed L-fuzzy topological space and  $(Y, \tau')$  be a hereditarily L-fuzzy iso-  $S^*$ -closed space. Let us consider the projection map  $P_Y : X \times Y \rightarrow Y$ .

Let  $\beta$  be a countably compact, closed L-fuzzy subset of  $X \times Y$ . Then  $P_Y(\beta)$  is countably compact L-fuzzy subset of  $(Y, \tau')$ . Since  $(Y, \tau')$  is hereditarily iso-  $S^*$ -closed L-fuzzy topological space then  $P_Y(\beta)$  is L-fuzzy  $S^*$ -closed. Thus from 3.16,  $X \times P_Y(\beta)$  is L-fuzzy iso-  $S^*$ -closed. Since  $\beta$  is a countably compact and closed subset of  $X \times P_Y(\beta) \leq X \times Y$ ,  $\beta$  is L-fuzzy  $S^*$ -closed subset of  $X \times Y$ . Hence  $X \times Y$  is L-fuzzy iso-  $S^*$ -closed.

**Definition 3.19**<sup>12</sup> An L-fuzzy topological space  $(X, \tau)$  is said to be extremally disconnected if and only if  $cl(\lambda) \in \tau$  for every  $\lambda \in \tau$ .

Kudri<sup>14</sup> established a relation among semi-compact space, s-closed and  $S^*$ -closedness in L-fuzzy topological spaces.

**Proposition 3.20**<sup>14</sup> Semi-compactness  $\Rightarrow S^*$ -closedness  $\Rightarrow S$ -closedness.

**Theorem 3.21**

Let  $(X, \tau)$  be an L-fuzzy topological space. Then the following relations hold.  $(X, \tau)$  is Semi-iso-compact  $\Rightarrow (X, \tau)$  is iso- $S^*$ -closed  $\Rightarrow (X, \tau)$  is iso- $S$ -closed.

**Proof:** The proof immediately follows from the proposition [3.20].

**Theorem 3.22**<sup>4</sup>

Let  $(X, \tau)$  be an extremally disconnected L-fuzzy topological space and  $\lambda \in L^X$ . Then the following are equivalent :

- i)  $\lambda$  is almost compact<sup>12</sup>.
- ii)  $\lambda$  is nearly compact<sup>14</sup>.
- iii)  $\lambda$  is S-closed.
- iv)  $\lambda$  is S\*-closed.
- v)  $\lambda$  is SS-closed<sup>4</sup>.

**Theorem 3.23**

Let  $(X, \tau)$  be an extremally disconnected L-fuzzy topological space and  $\lambda \in L^X$ . Then the following are equivalent :

- i)  $\lambda$  is weakly iso-compact<sup>6</sup>.
- ii)  $\lambda$  is nearly iso-compact<sup>7</sup>.
- iii)  $\lambda$  is iso-S-closed.
- iv)  $\lambda$  is iso- S\*-closed.
- v)  $\lambda$  is iso-SS-closed<sup>9</sup>.

**Proof:**First of all, we show that (i)  $\Rightarrow$ (ii). Suppose,  $(X, \tau)$  is weakly iso-compact and extremally disconnected L-fuzzy topological space. Let  $\lambda$  be a regular closed, countably almost compact L-fuzzy subset of  $(X, \tau)$ . Since countably almost compact extremally disconnected L-fuzzy topological space is countably nearly compact then  $\lambda$  is countably nearly compact. As  $(X, \tau)$  is L-fuzzy weakly isocompact,  $\lambda$  is almost compact and hence nearly compact ( almost compact extremally disconnected L-fuzzy topological space is nearly compact ). Hence  $(X, \tau)$  is nearly isocompactL-fuzzy topological space.

(ii)  $\Rightarrow$ (iii), (iii)  $\Rightarrow$ (iv), (iv)  $\Rightarrow$ (v) and (v)  $\Rightarrow$ (i) can be proved similarly.

**Corollary 3.24**<sup>4</sup>Let  $(X, \tau)$  be an extremally disconnected L-fuzzy topological space. If  $\lambda \in L^X$  is compact then  $\lambda$  is S-closed(S\*-closed).

**Corollary 3.25**Let  $(X, \tau)$  be an extremally disconnected L-fuzzy topological space. If  $\lambda \in L^X$  is iso-compact then  $\lambda$  is iso-S-closed (iso-S\*-closed).

**Proof:** Let  $\lambda$  be a closed countably compact L-fuzzy subset in  $(X, \tau)$ . Since it is isocompact then  $\lambda$  is compact. From 3.24, an extremally disconnected compact space is S-closed ( $S^*$ -closed) and so  $\lambda$  is S-closed ( $S^*$ -closed) and consequently it is iso-S-closed (iso- $S^*$ -closed).

#### 4. CL- ISO-S-CLOSEDNESS AND CL- ISO- $S^*$ -CLOSEDNESS IN L-FUZZY TOPOLOGICAL SPACES

M.Sakai<sup>16</sup> introduced and studied CL-isocompactness (spaces in which closure of each countably compact subspace is compact) in classical topology. In this section considering the S-closedness and  $S^*$ -closedness in L-fuzzy topological spaces, a generalized stronger form of iso-S-closedness and iso- $S^*$ -closedness are introduced and these new class of L-fuzzy topological spaces are called L-fuzzy CL-iso-S-closed and CL-iso- $S^*$ -closed spaces. Some properties of these spaces are studied here.

**Definition 4.1** Let  $(X, \tau)$  be an L-fuzzy topological space. The L-fuzzy set  $\lambda \in L^X$  is said to be L-fuzzy CL-iso-S-closed if the closure of each L-fuzzy countably compact subspace of  $\lambda$  is L-fuzzy S-closed. If  $\lambda$  is the whole space, then we say that the L-fuzzy topological space  $(X, \tau)$  is L-fuzzy CL-iso-S-closed. Obviously every L-fuzzy CL-iso-S-closed spaces are L-fuzzy iso-S-closed.

##### **Theorem 4.2**

Let  $f : (X, \tau) \rightarrow (Y, \tau')$  be an L-fuzzy perfect, almost continuous and almost open mapping with  $f^{-1}(y)$  is finite for every  $y \in Y$ , from a CL-iso-S-closed space  $(X, \tau)$  onto an L-fuzzy topological space  $(Y, \tau')$ . Then  $(Y, \tau')$  is CL- iso-S-closed L-fuzzy topological space.

**Proof:** Let  $\beta$  be an L-fuzzy countably compact subset of  $(Y, \tau')$ . Since  $f$  is L-fuzzy perfect,  $f^{-1}(\beta)$  is L-fuzzy countably compact subset of  $(X, \tau)$ . As  $(X, \tau)$  is L-fuzzy CL-iso-S-closed then  $cl(f^{-1}(\beta))$  is L-fuzzy S-closed. Since  $f$  is L-fuzzy closed, continuous and onto then  $f(cl(f^{-1}(\beta))) = cl(f(f^{-1}(\beta))) = cl(\beta)$ , which implies  $cl(\beta)$  is L-fuzzy S-closed. Hence  $(Y, \tau')$  is L-fuzzy CL-iso-S-closed.

##### **Theorem 4.3**

Let  $(X, \tau)$  be a fully stratified L-fuzzy iso-S-closed space and  $(Y, \tau')$  be an L-fuzzy CL- iso-S-closed space such that  $X$  is product related to  $Y$ . Then  $X \times Y$  is L-fuzzy CL- iso-S-closed.

**Proof:** Let  $(X, \tau)$  be a fully stratified iso-S-closed L-fuzzy topological space and  $(Y, \tau')$  be an L-fuzzy CL- iso-S-closed space. Let  $P_X: X \times Y \rightarrow X$  and  $P_Y: X \times Y \rightarrow Y$  be the projection maps.

Let  $\beta$  be an L-fuzzy countably compact subset of  $X \times Y$ . Then  $P_Y(\beta)$  is L-fuzzy countably compact. By L-fuzzy CL- iso-S-closedness of  $(Y, \tau')$ ,  $cl(P_Y(\beta))$  is L-fuzzy S-closed in  $(Y, \tau')$ . But  $P_X(\beta)$  is L-fuzzy countably compact subset of  $X$ . Since  $X$  is fully stratified, then by 2.19,  $P_X$

is L-fuzzy perfect and so is L-fuzzy closed. So  $P_X(\beta)$  is L-fuzzy S-closed in X. Thus  $\text{cl}(\beta)$  is contained in the L-fuzzy S-closed space  $P_X(\beta) \times \text{cl}(P_Y(\beta))$  (by 3.5). Hence  $\text{cl}(\beta)$  is L-fuzzy S-closed, which follows that  $X \times Y$  is L-fuzzy CL-iso-S-closed.

**Definition 4.4** An L-fuzzy topological space  $(X, \tau)$  is called hereditarily CL-iso-S-closed if every subspace of it is CL-iso-S-closed.

**Theorem 4.5**

If an L-fuzzy topological space  $(X, \tau)$  is hereditarily CL-iso-S-closed then  $(X, \tau)$  is hereditarily iso-S-closed.

**Proof:** Since every CL-iso-S-closed L-fuzzy topological space is L-fuzzy iso-S-closed, the result follows immediately.

**Definition 4.6** Let  $(X, \tau)$  be an L-fuzzy topological space. The L-fuzzy set  $\lambda \in L^X$  is said to be L-fuzzy CL-iso-  $S^*$ -closed if the closure of each L-fuzzy countably compact subspace of  $\lambda$  is L-fuzzy  $S^*$ -closed. If  $\lambda$  is the whole space, then we say that the L-fuzzy topological space  $(X, \tau)$  is L-fuzzy CL-iso-  $S^*$ -closed.

Obviously every L-fuzzy CL-iso-  $S^*$ -closed spaces are L-fuzzy iso-  $S^*$ -closed.

**Theorem 4.7**

Let  $f : (X, \tau) \rightarrow (Y, \tau')$  be an L-fuzzy perfect and semi-irresolute mapping with  $f^{-1}(y)$  is finite for every  $y \in Y$ , from a CL-iso-  $S^*$ -closed space  $(X, \tau)$  onto an L-fuzzy topological space  $(Y, \tau')$ . Then  $(Y, \tau')$  is CL- iso-  $S^*$ -closed L-fuzzy topological space.

**Proof:** Let  $\beta$  be an L-fuzzy countably compact subset of  $(Y, \tau')$ . Since  $f$  is L-fuzzy perfect,  $f^{-1}(\beta)$  is L-fuzzy countably compact subset of  $(X, \tau)$ . As  $(X, \tau)$  is L-fuzzy CL-iso-  $S^*$ -closed then  $\text{cl}(f^{-1}(\beta))$  is L-fuzzy  $S^*$ -closed. Since  $f$  is L-fuzzy closed, continuous and onto then  $f(\text{cl}(f^{-1}(\beta))) = \text{cl}(f(f^{-1}(\beta))) = \text{cl}(\beta)$ , which implies  $\text{cl}(\beta)$  is L-fuzzy  $S^*$ -closed. Hence  $(Y, \tau')$  is L-fuzzy CL-iso-  $S^*$ -closed.

**Theorem 4.8**

Let  $(X, \tau)$  be a fully stratified L-fuzzy iso- $S^*$ -closed space and  $(Y, \tau')$  be an L-fuzzy CL- iso-  $S^*$ -closed space such that X is product related to Y. Then  $X \times Y$  is L-fuzzy CL- iso- $S^*$ -closed.

**Proof:** Let  $(X, \tau)$  be a fully stratified iso-  $S^*$ -closed L-fuzzy topological space and  $(Y, \tau')$  be an L-fuzzy CL- iso-  $S^*$ -closed space. Let  $P_X: X \times Y \rightarrow X$  and  $P_Y: X \times Y \rightarrow Y$  be the projection maps.

Let  $\beta$  be an L-fuzzy countably compact subset of  $X \times Y$ . Then  $P_Y(\beta)$  is L-fuzzy countably compact. By L-fuzzy CL- iso-  $S^*$ -closedness of  $(Y, \tau')$ ,  $\text{cl}(P_Y(\beta))$  is L-fuzzy  $S^*$ -closed in  $(Y, \tau')$ . But  $P_X(\beta)$  is L-fuzzy countably compact subset of  $X$ . Since  $X$  is fully stratified, then by 2.19,  $P_X$  is L-fuzzy perfect and so is L-fuzzy closed. So  $P_X(\beta)$  is L-fuzzy  $S^*$ -closed in  $X$ . Thus  $\text{cl}(\beta)$  is contained in the L-fuzzy  $S^*$ -closed space  $P_X(\beta) \times \text{cl}(P_Y(\beta))$  (by 3.15). Hence  $\text{cl}(\beta)$  is L-fuzzy  $S^*$ -closed, which follows that  $X \times Y$  is L-fuzzy CL-iso-  $S^*$ -closed.

**Definition 4.9** An L-fuzzy topological space  $(X, \tau)$  is called hereditarily CL-iso-  $S^*$ -closed if every subspace of it is CL-iso-  $S^*$ -closed.

**Theorem 4.10**

If an L-fuzzy topological space  $(X, \tau)$  is hereditarily CL-iso- $S^*$ -closed then  $(X, \tau)$  is hereditarily iso- $S^*$ -closed.

**Proof:** Since every CL-iso-  $S^*$ -closed L-fuzzy topological space is L-fuzzy iso-  $S^*$ -closed, the result follows immediately.

**CONCLUSION**

There are so many compactness in literature. At present, many authors are working on various forms of compactness in fuzzy topology as well as L-fuzzy topological spaces. Our intention is to generalize these compactness in L-fuzzy topological spaces and to establish relations with other spaces. As a result we have defined concepts iso- $S$ -closedness and iso-  $S^*$ -closedness and their stronger forms CL-iso- $S$ -closedness and CL-iso-  $S^*$ -closedness and got some important relations with other spaces. We feel that with the help of these spaces some more new spaces will be developed in future.

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